# Closed-Form Factorization of Latent Semantics in GANs

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### OUTLINE

### ► Authorship

- ► Background
- ► Proposed Method
- ► Experimental Results
- ► Conclusion

► GAN Generator  $\mathbf{I} = G(\mathbf{z})$ , z: d-dimensional latent; I: image

- ► PGGAN (ICLR-18)
- ► BigGAN (ICLR-19)
- ► StyleGAN (CVPR-19)

► GAN Generator  $\mathbf{I} = G(\mathbf{z})$ , z: d-dimensional latent; I: image

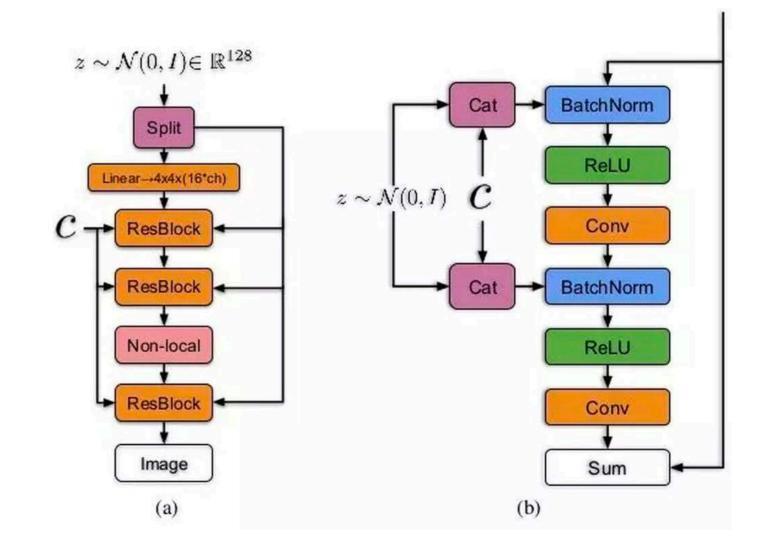
► PGGAN (ICLR-18) G Latent Latent Latent 4x4 4x4 4x4 ► BigGAN (ICLR-19) 8x8 ► StyleGAN (CVPR-19) 1024x1024 Reals Reals Reals D 1024x1024 8x8 4x4 4x4 4x4 Training progresses

► GAN Generator  $\mathbf{I} = G(\mathbf{z})$ , z: d-dimensional latent; I: image

► PGGAN (ICLR-18)

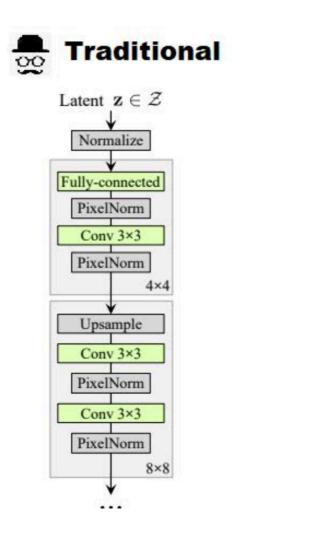
► BigGAN (ICLR-19)

► StyleGAN (CVPR-19)

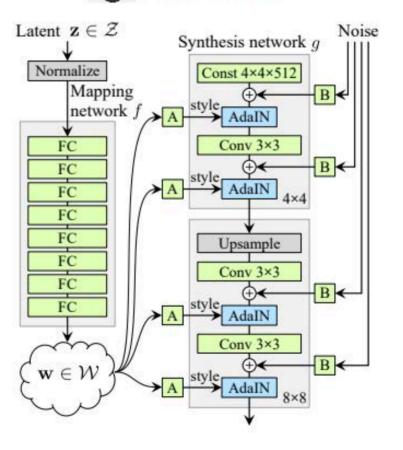


► GAN Generator  $\mathbf{I} = G(\mathbf{z})$ , z: d-dimensional latent; I: image

- > PGGAN (ICLR-18)
  > BigGAN (ICLR-19)
- ► StyleGAN (CVPR-19)



**StyleGAN** 



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- ► Authorship
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- ► Preliminaries
- GAN Generator  $\mathbf{I} = G(\mathbf{z})$ , z: d-dimensional latent; I: image
- Focus on the first step, since it is most relevant to the latent space we would like to explore

$$G_1(\mathbf{z}) \triangleq \mathbf{y} = \mathbf{A}\mathbf{z} + \mathbf{b}$$

- y: m-dimensional projected code
- A: weight
- b: bias

- ► Preliminaries
- Manipulation/Editing

$$\texttt{edit}(G(\mathbf{z})) = G(\mathbf{z}') = G(\mathbf{z} + \alpha \mathbf{n})$$

- n: a certain direction to represent a semantic concept
- a: the manipulation intensity

- Unsupervised Semantic Factorization
- Manipulation/Editing only consider the first projection step

$$\mathbf{y}' \triangleq G_1(\mathbf{z}') = G_1(\mathbf{z} + \alpha \mathbf{n})$$
$$= \mathbf{A}\mathbf{z} + \mathbf{b} + \alpha \mathbf{A}\mathbf{n} = \mathbf{y} + \alpha \mathbf{A}\mathbf{n}$$

• Find directions that can cause large variations

$$\mathbf{n}^* = rgmax_{\{\mathbf{n}\in\mathbb{R}^d:\ \mathbf{n}^T\mathbf{n}=1\}} ||\mathbf{A}\mathbf{n}||_2^2$$

• If An = 0, the editing will keep the output unchanged

- Unsupervised Semantic Factorization
- Find the k most important directions

$$\mathbf{N}^* = \max_{\{\mathbf{N} \in \mathbb{R}^{d \times k}: \mathbf{n}_i^T \mathbf{n}_i = 1 \forall i = 1, \cdots, k\}} \sum_{i=1}^k ||\mathbf{A}\mathbf{n}_i||_2^2$$

• How to solve? Lagrange multipliers

$$egin{aligned} \mathbf{N}^* &= rg\max_{\mathbf{N}\in\mathbb{R}^{d imes k}}\sum_{i=1}^k ||\mathbf{A}\mathbf{n}_i||_2^2 - \sum_{i=1}^k \lambda_i (\mathbf{n}_i^T\mathbf{n}_i-1) \ &= rg\max_{\mathbf{N}\in\mathbb{R}^{d imes k}}\sum_{i=1}^k (\mathbf{n}_i^T\mathbf{A}^T\mathbf{A}\mathbf{n}_i - \lambda_i\mathbf{n}_i^T\mathbf{n}_i + \lambda_i) \end{aligned}$$

Unsupervised Semantic Factorization

$$\arg \max_{\mathbf{N} \in \mathbb{R}^{d \times k}} \sum_{i=1}^{k} (\mathbf{n}_{i}^{T} \mathbf{A}^{T} \mathbf{A} \mathbf{n}_{i} - \lambda_{i} \mathbf{n}_{i}^{T} \mathbf{n}_{i} + \lambda_{i})$$

• Take the partial derivative on each n<sub>i</sub>

 $2\mathbf{A}^T \mathbf{A} \mathbf{n}_i - 2\lambda_i \mathbf{n}_i = 0$ 

• Solutions are the eigenvectors of the matrix  $\mathbf{A}^T \mathbf{A}$ 

• The proposed method is called **SeFa** (Semantic Factorization)

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- Results on Diverse Models and Datasets
- Comparison with Supervised Approach
- Comparison with Unsupervised Baselines
- ► Real Image Editing

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### EXPERIMENTAL RESULTS

### Interactive Editing by Tuning Interpretable Directions



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### **EXPERIMENTAL RESULTS**

#### Interactive Editing by Tuning Interpretable Directions

#### Posture (Left & Right)



#### Posture (Up & Down)



Zoom



### Interactive Editing by Tuning Interpretable Directions



Orientation

#### Vertical Position



#### Shape



# SeFa: Closed-Form Factorization of Latent Semantics in GANs

# **Demo Video**

Yujun Shen, Bolei Zhou The Chinese University of Hong Kong

- ► Results on StyleGAN
- ► Cars:
- Bottom layers rotation
- Middle layers shape
- Top layers color

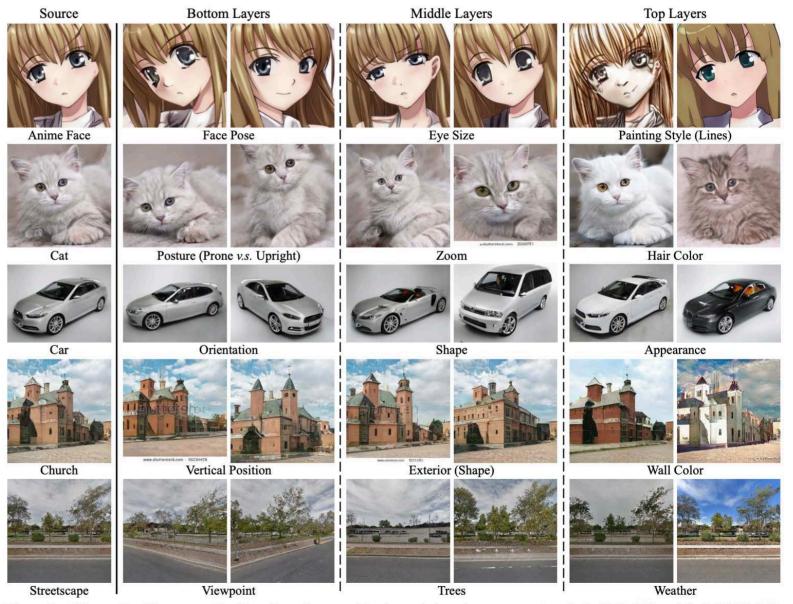


Figure 2. Hierarchical interpretable directions discovered in the style-based generators, *i.e.*, StyleGAN [17] and StyleGAN2 [18]. Among them, the streetscapes model is trained with StyleGAN2, while the others are using StyleGAN.

► SeFa can indeed find human-understandable concepts

Table 1. User study. We randomly generate 2K images for each dataset, and use the Top-50 eigen directions from each level of layers to manipulate these images. Numbers in brackets indicate the index of the layers to interpret. Users are asked how many directions result in *obvious* content change (numerator) and how many directions are semantically meaningful (denominator).

Dataset	Bottom (0-1)	Middle (2-5)	Top (6-)
Anime Face [1]	12/12	26/26	38/50
LSUN Cat [27]	14/15	21/28	47/50
LSUN Car [27]	10/10	16/22	22/34
LSUN Church [27]	15/15	18/26	48/50
Streetscape [20]	9/9	12/18	15/36

### ► Results on BigGAN

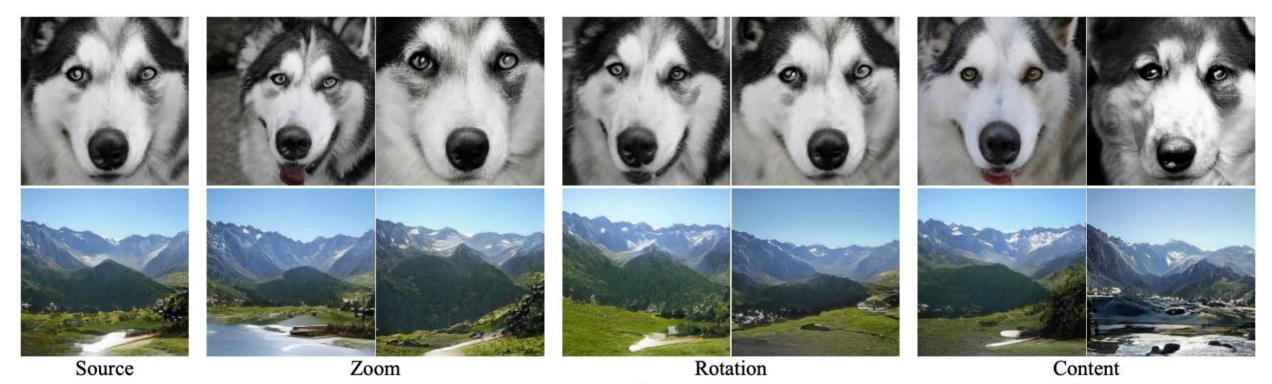


Figure 3. Diverse interpretable directions found in the BigGAN [4], which is conditionally trained on ImageNet [6]. These semantics are further used to manipulate images from different categories.

Results on Diverse Models and Datasets

- Comparison with Supervised Approach
- Comparison with Unsupervised Baselines
- ► Real Image Editing

- Comparison with Supervised Approach
- ► InterFaceGAN (CVPR-20) with well defined facial attributes
  - Requires sampling numerous data and pre-training attribute predictors

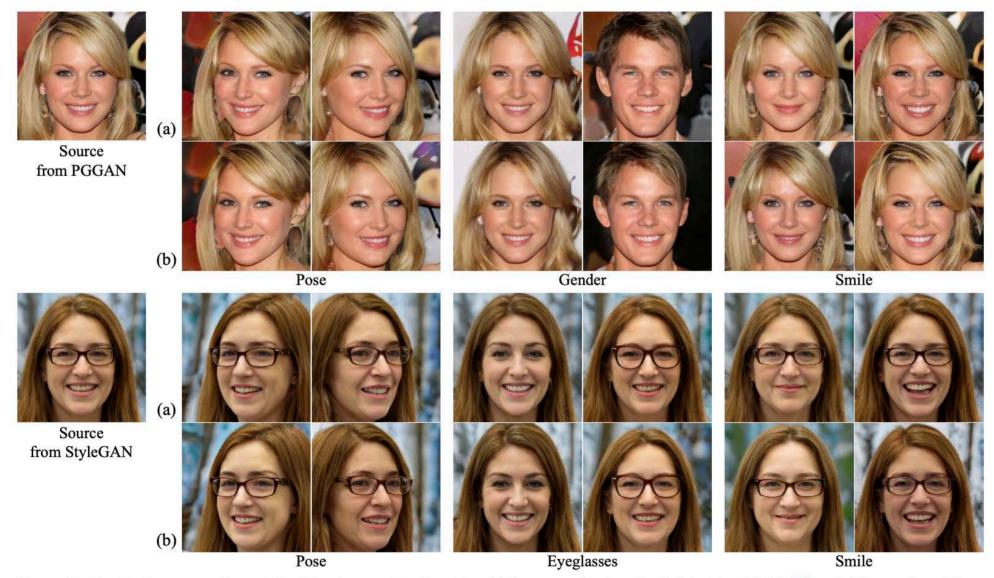


Figure 5. Qualitative comparison of the latent semantics found by (a) the supervised method, InterFaceGAN [24] and (b) our *closed-form* solution, SeFa, where SeFa achieves similar performance to InterFaceGAN. PGGAN trained on CelebA-HQ [16] and StyleGAN trained on FF-HQ [17] are used as the target models to interpret.

- ► Train an attribute predictor on CelebA with ResNet50
- Quantitatively evaluate whether the identified directions can properly represent the corresponding attributes

Table 2. **Re-scoring analysis** of the semantics identified by InterFaceGAN [24] and SeFa from the PGGAN model trained on CelebA-HQ dataset [16]. Each row evaluates how the semantic scores change after moving the latent code along a certain direction.

(a) 1	(a) InterfaceOAN [24], which is supervised.					
	Pose	Gender	Age	Glasses	Smile	
Pose	0.53	-0.06	-0.09	-0.01	0.05	
Gender	-0.02	0.59	0.20	0.08	-0.07	
Age	-0.03	0.35	0.50	0.08	-0.03	
Glasses	-0.01	0.37	0.19	0.24	0.00	
Smile	-0.01	-0.07	0.03	-0.01	0.60	

(a) InterFaceGAN [24] which is supervised

(b) SeFa, which is unsupervised.

	Pose	Gender	Age	Glasses	Smile
Pose	0.51	-0.11	-0.07	0.02	0.06
Gender	0.02	0.55	0.46	0.09	-0.13
Age	-0.07	-0.25	0.34	0.10	0.10
Glasses	0.02	0.55	0.46	0.09	-0.13
Smile	0.03	-0.03	0.15	-0.16	0.42

• SeFa can adequately control some attribute similar to InterFaceGAN.

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Glasses	-0.01	0.37	0.19	0.24	0.00	Glasses	
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• When altering one semantic, InterFaceGAN shows stronger robustness to other attributes, benefiting from its supervised training manner.

- ► Train an attribute predictor on CelebA with ResNet50
- Quantitatively evaluate whether the identified directions can properly represent the corresponding attributes

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- SeFa fails to discover the direction corresponding to eyeglasses.
- The presence of eyeglasses is not a large variation.

- ► SeFa can find more diverse semantics in the latent space
- Hair color, hair style, and brightness (not easy to acquire)
- More complex attributes

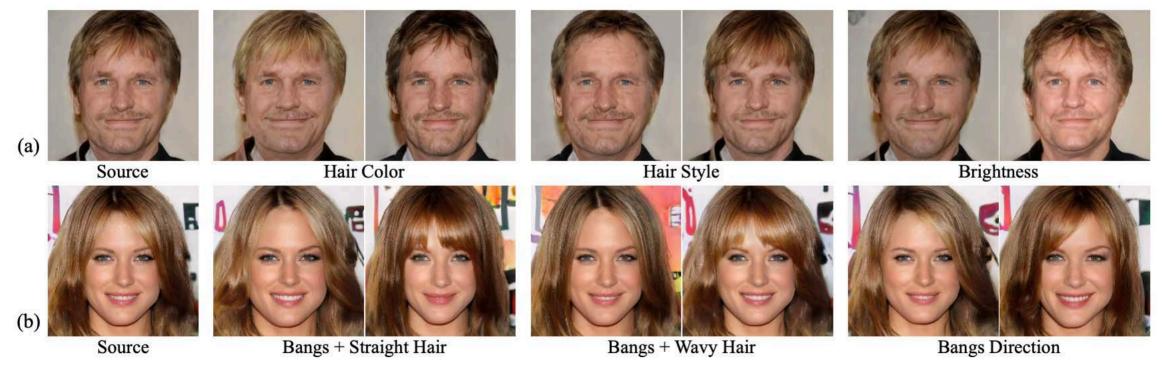
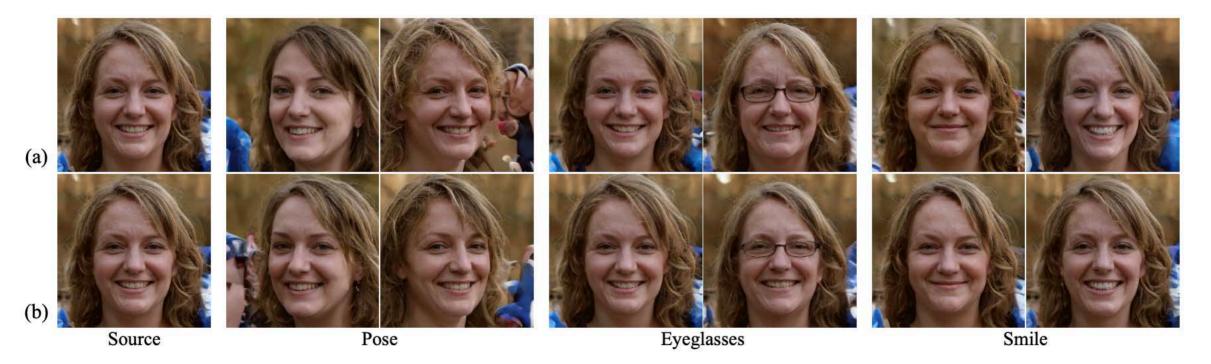


Figure 6. (a) Diverse semantics, which can *not* be identified by InterFaceGAN [24] due to the lack of semantic predictors. (b) Diverse hair styles, which can *not* be described as a binary attribute. The PGGAN model trained on CelebA-HQ dataset [16] is used.

- Results on Diverse Models and Datasets
- Comparison with Supervised Approach
- Comparison with Unsupervised Baselines
- ► Real Image Editing

- Comparison with Unsupervised Baselines
- Sampling-based Baseline
- GANSpace (NeurIPS-20): PCA on a collection of sampled data



The semantics found by SeFa lead to a more precise control

- Comparison with Unsupervised Baselines
- Sampling-based Baseline
- GANSpace (NeurIPS-20): PCA on a collection of sampled data

	FID	Re-scoring	User Study
GANSpace [10]	7.43	0.33	41%
SeFa (Ours)	7.36	0.38	59%

- Comparison with Unsupervised Baselines
- Learning-based Baseline
- InfoGAN (NeurIPS-16): use a regularizer to maximize the mutual information between the output image and the input latent code

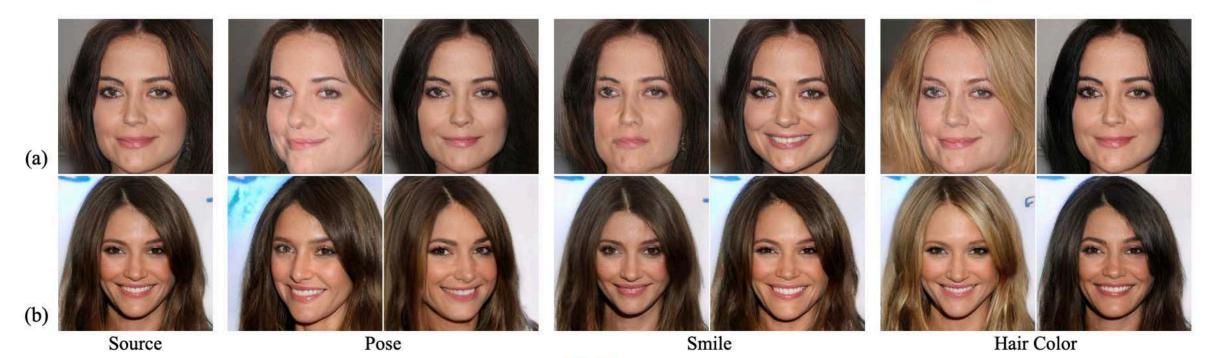


Figure 8. Qualitative comparison between (a) Info-PGGAN [21, 5] and (b) SeFa. The result of the Info-PGGAN model is extracted directly from [21], and the official PGGAN model trained on CelebA-HQ dataset [16] is used for SeFa.

- Results on Diverse Models and Datasets
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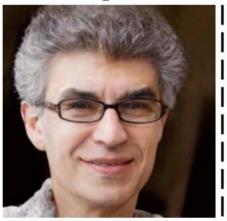
- ► Real Image Editing
- Given a target image to edit, first project it back to the latent space, then use the variation factor found by SeFa to modulate



Pose

Input

Smile



Inversion

Eyeglasses



Gender

Figure 9. **Real image editing** with respect to various facial attributes. All semantics are found with the proposed SeFa. GAN inversion [28] is used to project the target real image back to the latent space of StyleGAN [17].

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### CONCLUSION

- ► Factorizing the latent semantics learned by GANs
- Identifying versatile semantics from different types of GAN models in an unsupervised manner